

summer term mathematics activities for year six

Here is an oblong (rectangle) 3 squares long and 2 squares wide.

You have three smaller squares. The smaller squares fit in the oblong.

How many different ways can you fit the 3 smaller squares in the large oblong so that half the oblong is shaded?

Rotations and reflections count as the same shape.





The two above count as the same possibility

There are six possibilities

The solution is on the next slide



Did you find them all?





A visualisation problem:

A model is made from cubes as shown.



How many cubes make the model? A part of how many cubes can you see?

How many cubes can't you see?

If the cubes were arranged into a tower what is the most number of the square faces could you see at one time?

Answer



How many cubes make the model?

How many part cubes can you see?













If the cubes were arranged into a tower what is the most number of the square faces could you see at one time?







You have 4 equilateral triangles.

How many different shapes can you make by joining the edges together exactly?



How many of your shapes will fold up to make a tetrahedron?



You can make three shapes





Two make the net of a tetrahedron

How many oblongs (rectangles) are there altogether in this drawing?





How many oblongs (rectangles) are there altogether in this drawing?

Look at the available oblongs (rectangles). Colour indicates size. Number of each type shown



Answer

How many oblongs (rectangles) are there altogether in this drawing?

The rectangles may be counted on the grid

E.g. there are 4 oblongs 2 sections wide and 3 sections long



60

Draw as many different quadrilaterals as you can on a 3 \times 3 dot grid.

One has been done for you.



Use a fresh grid for each new quadrilateral.

Repeats of similar quadrilaterals in a different orientation do not count.

There are 16 possibilities. Can you find them all?



Finding all possibilities: 16 Quadrilaterals



Answer

Adding to make twenty:



Add any four digits to make the total 20

There are 12 possible solutions - can you find the other 11?



Making twenty:

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7	8	9

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Answer

Adding to make twenty - ANSWERS:







Finding cubes of numbers

To find the cube of a number multiply the number by itself and multiply your answer again by the number,

e.g. $3 \times 3 \times 3$ becomes $3 \times 3 = 9$ $9 \times 3 = 27$

27 is a cube number without a decimal. 3 \times 3 \times 3 is sometimes written as; 3³ or 3 to the power 3.



Find the cubes of these numbers:

2	2 x 2 x 2	=	8
5	5 x 5 x 5	=	125
9	9 x 9 x 9	=	729
10	10 × 10 × 10	=	1000



Now find the cubes of the numbers 10 to 21

10	10 x	10 x	10 =	1000
11	11 ×	11 ×	11 =	1331
12	12 x	12 x	12 =	1728
13	13 x	13 x	13 =	2197
14	14 x	14 x	14 =	2744
15	15 x	15 x	15 =	3375
16	16 x	16 x	16 =	4096
17	17 x	17 x	17 =	4913
18	18 x	18 ×	18 =	5832
19	19 x	19 x	19 =	6859
20	20 x	20 >	< 20 =	8000
21	21 x	21 x	21 =	9261



Now use the cubes of the numbers 10 to 21

100013311728219727443375409649135832685980009261

These cube numbers are the only ones with four digits

Arrange the numbers on the grid in cross number fashion.





Answer

Find the link:

The set of numbers below are linked by the same mathematical process.



Try these

Answer: Add 4 to the top box and multiply your answer by 7.

Find the process ... mild



Add 2 and multiply by 4

С

Add 2 and subtract 6



Multiply by 3 and add 10

Divide by 7 and add 5 Answer

Find the process ... moderate



Subtract 13 and divide by 9 Square the number and + 34



Divide by 5 and halve the answer

Divide by 11 and add 45 Answer

Find the process ... more taxing



Find square root & subtract 7 Add 12 & multiply by 5



Finding cube numbers

Multiply by 1000 and find a $\frac{1}{4}$ Answer Co-ordinate words

The grid shows letters at certain co-ordinates.

Look at the groups of co-ordinates and identify the hidden words.





Give co-ordinates for MODE [3,2] [6,4] [-2,7] [-7,4]



[-5,-5] [-6,5] [-1,2] [-5,1] [1,2]

Give co-ordinates for TRIANGLE [3,-3][-1,-3][-6,5][5,-4][-1,2][1,-1][1,-5][-3,-4]Answer

MIINUS

Arranging numbers around squares ... Here are nine numbers.

Arrange eight of them in the blank squares so that the sides make the total shown in the circle. Each number may be used once only. E.G.



Arranging numbers around squares ... Here are nine numbers.

Arrange eight of them in the blank squares so that the sides make the total shown in the circle.





Arranging numbers around squares ... Here are nine numbers.

Arrange eight of them in the blank squares so that the sides make the total shown in the circle. E.G.



Nets of a cube ...

A cube may be unfolded in many different ways to produce a net.



Each net will be made up of six squares.

There are 11 different ways to produce a net of a cube. Can you find them all?



Answer

More _____

Nets of a cube the final five ...




Rugby union scores ...

In a rugby union match scores can be made by the following methods:

A try and a conversion	7 points
A try not converted	5 points
A penalty goal	3 points
A drop goal	3 points

Rugby union scores ...

In a rugby union match scores can be made by the following methods:

A try and a conversion	7 points
A try not converted	5 points
A penalty goal	3 points
A drop goal	3 points

In a game Harlequins beat Leicester by 21 points to 18.

The points were scored in this way:

Harlequins: 1 converted try, 1 try not converted, 2 penalties and a drop goal.

Leicester: 3 tries not converted and a drop goal.

Are there any other ways the points might have been scored?



The display shows a time on a digital clock.



It uses different digits

The time below displays the same digit



There are two other occasions when the digits will be the same on a digital clock.

Can you find them?





The occasions when digital clock displays the same digit are.





The displays show time on a digital clock.



The display shows 2 different digits, each used twice.

Can you find all the occasions during the day when the clock will display 2 different digits twice each?

There are forty-nine altogether

Look for a systematic way of working



Two digits appearing twice on a digital clock.



0	4	4	0
C	5	0	5
C	5	5	0
C	6	0	6
C	7	0	7
C	8	0	8
C	9	0	9
1	0	0	1
1	0	1	0
1	1	0	0
1	1	2	2
1	1	3	3





Triangle test

Each of the triangles below use the same rule to produce the answer in the middle.



Can you find the rule?



Triangle test

Each of the triangles below use the same rule to produce the answer in the middle.



Add the two bottom numbers and subtract the top one

Try these using the same rule •



Using the same rule can you find which numbers fit at the missing apex of each triangle?



Triangle test



Multiply the top number by the one on the left and subtract the number on the right. This will give you the number in the centre.

TASK: Create some triangle sequences for yourself and ask your friends to find the rule you have used.

Nine dots

Nine dots are arranged on a sheet of paper as shown below.



TASK: Start with your pencil on one of the dots. Do not lift the pencil from the paper. Draw four straight lines that will connect all the dots

Click for help 1 🔵 Start with a dot in a corner

Click for help 2 The line does not have to finish on a dot



Nine dots

Nine dots are arranged on a sheet of paper as shown below.

Start here





TASK: Start with your pencil on one of the dots. Do not lift the pencil from the paper. Draw four straight lines that will connect all the dots Fifteen coins make a pound.

How many different combinations of 15 coins can you find that will make exactly ± 1 ?

Coins may be used more than once.

Click when you need help

TRY: starting with two fifty pence pieces and cascading [changing them] coins until you reach £1 with 15 coins.

THINK: Once you have found one combination change coins to find others.



Fifteen coins make a pound.

A couple of possibilities:

1	×	50p	-	50p
9	×	5p	- 4	45p
5	×	1p	-	5р
15	coins	totalling	£1.00	

1	×	50p	-	50p
1	×	20p	-	20p
1	×	10p	-	10p
2	×	5p	-	10p
10	×	1р	-	10p
15	coins	totalling	£1.	00

Have you found any others?

The exchange rate for marbles is as follows:

- **3** GREEN marbles has the same value as **5** BLUE marbles
- 2 RED marbles have the same value as 1 PURPLE marble
- 4 RED marbles have the same value as 3 GREEN marbles

How many **BLUE** marbles can you get for **8 PURPLE** marbles?



TRY: using marbles to represent exchanges.



Marble exchange

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Start answer sequence

- 1 purple = 2 red.
- 8 purple = 16 red
- 4 red = 3 green so 16 red = 12 green.
- 3 green = 5 blue so 12 green = 20 blue
- You can get 20 blue marbles for 8 purple ones

Counters.



Jack has four different coloured counters. He arranges them in a row. How many different ways can he arrange them? One has been done for you.



There are 24 possible combinations.



Counters.

Click to start answer sequence



Domino sequences.

Find the next two dominoes in each of these sequences.



Domino sequences.

Find the next two dominoes in each of these sequences.



Domino squares.



The four dominoes above are arranged in a square pattern.

Each side of the pattern adds up to 12.

How might the dominoes be arranged?

Are there any other possible solutions?

Can you find four other dominoes that can make a number square?



Dominoes puzzle:



Rearrange these dominoes in the framework below so that the total number of spots in each column adds up to 3 and the total of each row is 15. Draw spots to show how you would do it.





Dominoes puzzle answer:



Rearrange these dominoes in the framework below so that the total number of spots in each column adds up to 3 and the total of each row is 15



The arrangement of dominoes may vary as long as the totals remain correct



Dominoes puzzle:



Rearrange these dominoes in the framework below so that the total number of spots in each column adds up to 4 and the total of each row is 8. Draw spots to show how you would do it.





Dominoes puzzle:



Rearrange these dominoes in the framework below so that the total number of spots in each column adds up to 4 and the total of each row is 8. Draw spots to show how you would do it.



Other arrangements of this framework may be possible



Patio pathways

Jodie is making a patio.

She uses red tiles and white tiles.

She first makes an L shape with equal arms from red slabs.

She then puts a grey border around the patio.

The smallest possibility has been done for you.



Draw the next <u>four</u> patios and record your results in the table

Patio pathways



Predict how many grey slabs you will see if the arm length was 9 slabs.



Number squares





What if we used ... ? Subtraction Multiplication Division

Playing with consecutive numbers.

The number 9 can be written as the sum of consecutive whole numbers in two ways.

9 = 2 + 3 + 4 9 = 4 + 5

Think about the numbers between 1 and 20. Which ones can be written as a sum of consecutive numbers?

Which ones can't?

Can you see a pattern?

What about numbers larger than 20?

Playing with consecutive numbers.

- 15 = 7 + 8 15 = 1 + 2 + 3 + 4 + 515 = 4 + 5 + 6
- What about 1, 2, 4, 8, 16? What about 32? 64?





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You have 4 equilateral triangles.

How many different shapes can you make by joining the edges together exactly?



How many of your shapes will fold up to make a tetrahedron?

How many rectangles are there altogether in this drawing?



Draw as many different quadrilaterals as you can on a 3 \times 3 dot grid.

•<

Use a fresh grid for each new quadrilateral.
ullet	lacksquare	•	ullet	lacksquare	\bullet	lacksquare	ullet	\bullet	lacksquare	lacksquare	lacksquare
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ullet	lacksquare	•	\bullet	lacksquare	\bullet	lacksquare	ullet	\bullet	lacksquare	lacksquare	lacksquare
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27 is a cube number without a decimal.

 $3 \times 3 \times 3$ is sometimes written as;

 3^3 or 3 to the power 3.

Find the cubes of these numbers:



Now find the cubes of the numbers 10 to 21



Find the process ... mild





Find the process ... moderate





Find the process ... more taxing





[8,4] [1,7] [7,1] [7,5] [3,0] [8,2] [2,3] [6,6] [6,1] [1,5] [7,3] [6,6] [8,6]

[7,5] [3,0] [8,2] [7,5]





[-4,8] [-4,3] [6,4] [3,2] [5,3] [-8,7] [2,4] [-6,6] [-3,5] [6,7] [-8,2] [-7,4] [6,4] [5,3] [-8,2] [6,4] [-3,5] [6,7] [-4,3] [-7,4] [7,6] [-6,6] [6,7] [6,4] [-3,5]

Give co-ordinates for MODE



[-4,-1] [5,-4] [3,3] [3,-3] [4,-2] [-1,-3] [-3,-4] [3,1] [-5,1] [5,-4] [1,-5] [-5,-5] [-6,5] [-1,2] [-5,1] [1,2]

Give co-ordinates for TRIANGLE

Arranging numbers around squares ... Here are nine numbers.

8 9 7 3 5 2 15 16 11

Arrange eight of them in the blank squares so that the sides make the total shown in the circle.



Arranging numbers around squares ... Here are nine numbers.

30 33 37 34 32 36 35 31 38

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Nets of a cube ...

A cube may be unfolded in many different ways to produce a net.



Each net will be made up of six squares.

There are 11 different ways to produce a net of a cube. Can you find them all? Rugby union scores ...

In a rugby union match scores can be made by the following methods:

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In a game Harlequins beat Leicester by 21 points to 18. How might the points have been scored?

Are there any other ways the points might have been scored?

DIGITAL CLOCK

The displays show time on a digital clock.



The display shows 2 different digits, each used twice.

Can you find all the occasions during the day when the clock will display 2 different digits twice each?

There are forty-nine altogether

Look for a systematic way of working

Two digits appearing twice on a digital clock.



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Can you find the rule?



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What if we used ... ?

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Multiplication

Division

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